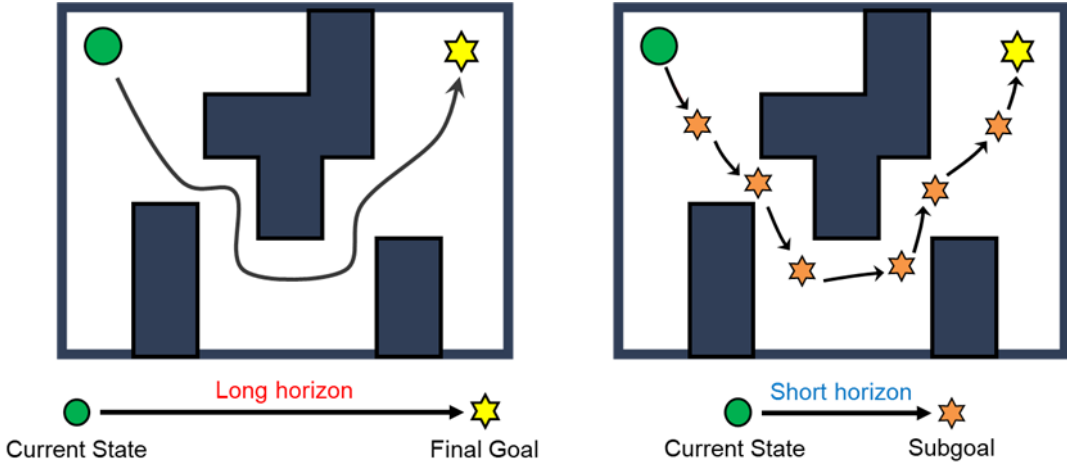




Graph-Assisted Stitching for Offline Hierarchical Reinforcement Learning

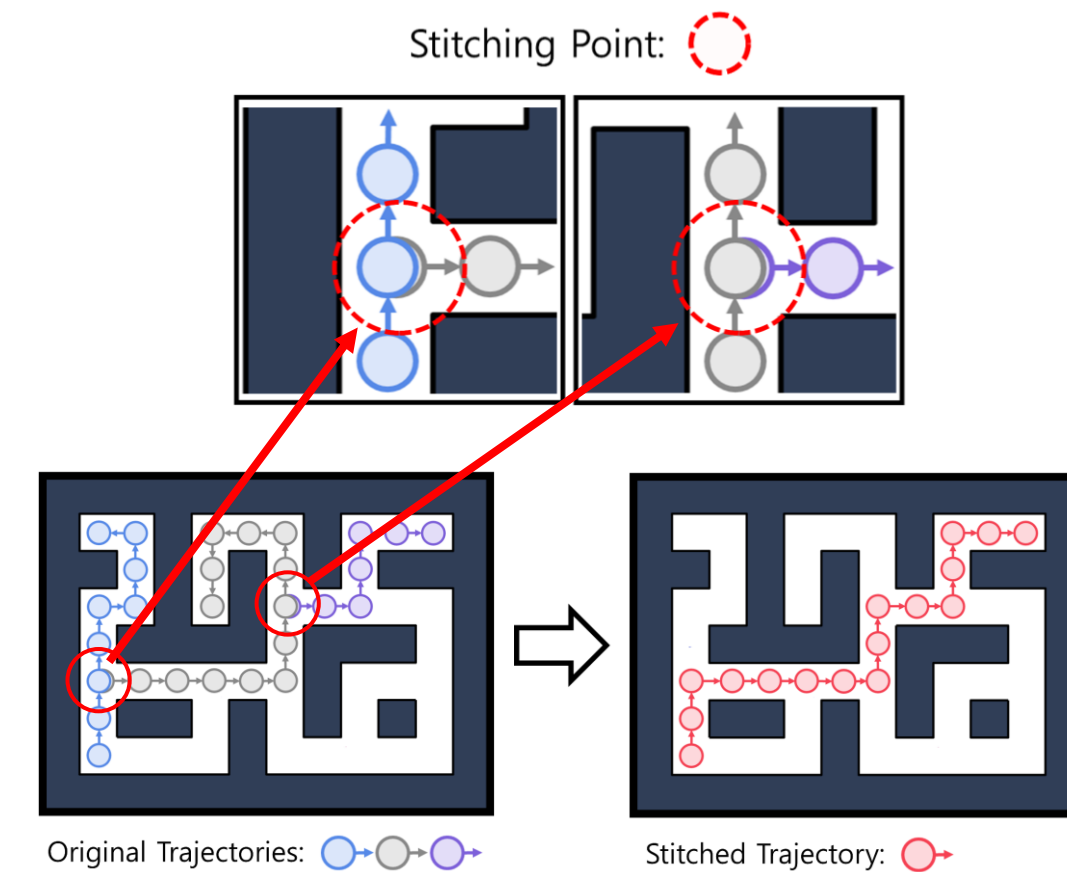
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Introduction



- Offline HRL introduces a two-level decision-making framework, where a **high-level policy** generates **subgoals** and a low-level policy executes primitive actions to reach them.
- This hierarchical structure decomposes complex **long-horizon** problems into manageable **short-horizon** subproblems.

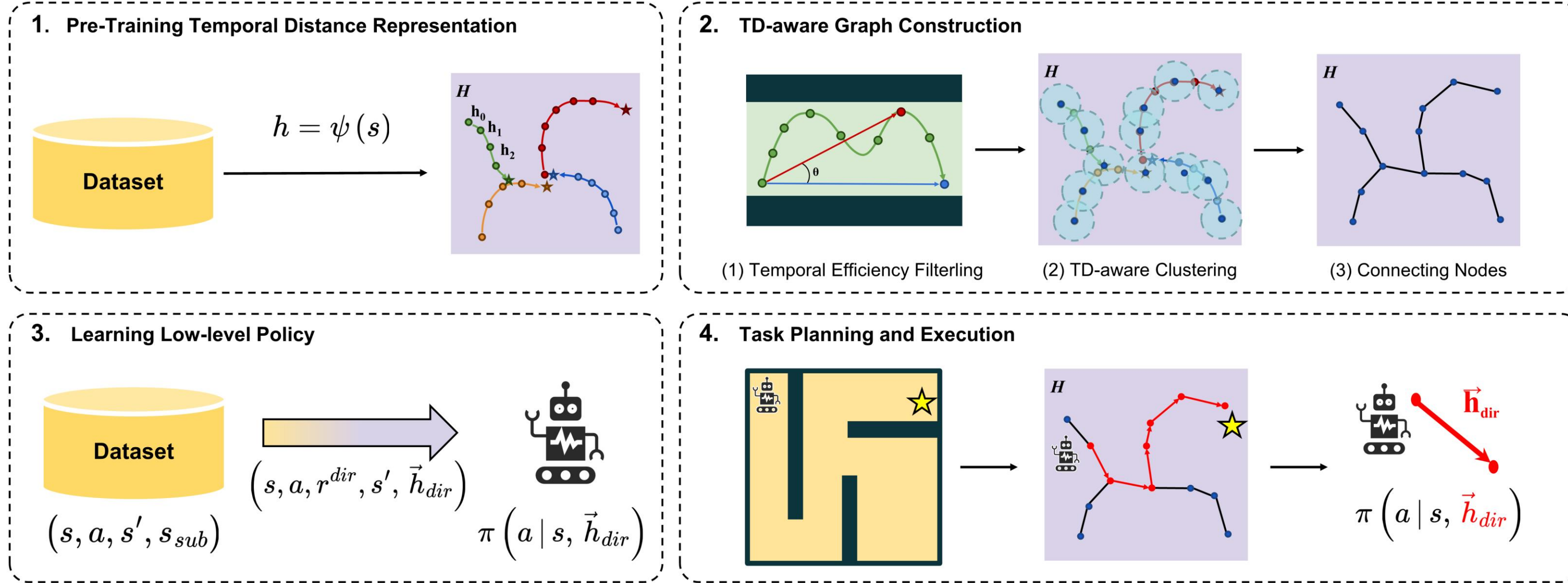
Motivation



Why is Trajectory Stitching Crucial in Offline HRL?

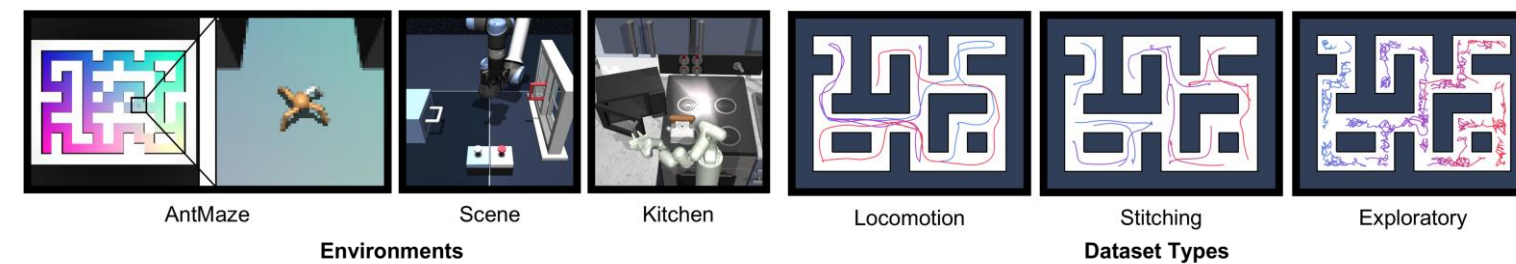
- Stitching composes new trajectories by connecting partial segments from different goal-oriented trajectories.
- This enables agents to utilize transitions that are **temporally disjoint** and **not observed within a single trajectory**.
- Such stitching facilitates generalization across goals, especially in sparse-reward and long-horizon tasks.
- However, **existing offline HRL methods** typically lack mechanisms for **cross-goal stitching**, limiting their ability to compose effective subgoal sequences from suboptimal trajectories.

Overview of GAS



Experiments

Datasets



Benchmark results: state-based environments

Dataset Type	Dataset	GCBC	GCIQL	QRL	CRL	HGCB	HHILP	HIQL	GAS (ours)
Locomotion	antmaze-medium-navigate	33.1 ± 5.6	74.6 ± 4.8	81.9 ± 8.2	95.3 ± 1.0	58.1 ± 5.5	96.3 ± 0.4	95.3 ± 1.3	96.3 ± 1.3
	antmaze-large-navigate	23.4 ± 3.2	32.6 ± 4.7	74.9 ± 4.4	85.5 ± 5.3	44.3 ± 4.1	86.8 ± 3.6	93.2 ± 2.2	93.2 ± 0.5
	antmaze-giant-navigate	0.0 ± 0.0	0.1 ± 0.4	14.3 ± 3.6	15.0 ± 5.7	7.2 ± 1.7	53.1 ± 2.6	67.3 ± 5.5	77.6 ± 2.9
Stitching	antmaze-medium-stitch	43.2 ± 7.7	26.6 ± 6.8	67.0 ± 10.6	57.0 ± 7.9	65.9 ± 5.7	96.0 ± 1.2	92.0 ± 2.8	98.1 ± 1.2
	antmaze-large-stitch	2.3 ± 3.6	9.6 ± 3.1	20.2 ± 1.7	14.4 ± 5.9	10.7 ± 5.8	34.1 ± 3.0	71.7 ± 4.8	96.3 ± 0.9
	antmaze-giant-stitch	0.0 ± 0.0	0.0 ± 0.0	0.4 ± 0.3	0.0 ± 0.0	0.0 ± 0.0	0.0 ± 0.0	1.0 ± 1.2	88.3 ± 3.6
Exploratory	antmaze-medium-explore	2.7 ± 2.8	11.7 ± 1.3	1.4 ± 1.2	1.0 ± 1.6	15.0 ± 8.2	39.9 ± 7.4	32.2 ± 3.0	98.1 ± 0.4
	antmaze-large-explore	0.0 ± 0.0	0.6 ± 0.5	0.3 ± 1.0	0.0 ± 0.0	0.0 ± 0.0	2.4 ± 1.9	2.9 ± 4.3	94.2 ± 3.0
Manipulation	scene-play	5.4 ± 0.9	50.4 ± 1.4	5.1 ± 1.7	19.2 ± 3.0	4.6 ± 1.3	43.4 ± 5.2	40.0 ± 9.6	73.6 ± 8.0
	kitchen-partial	69.5 ± 14.1	55.6 ± 17.5	61.9 ± 8.5	32.7 ± 11.7	71.1 ± 6.2	66.7 ± 9.0	73.1 ± 2.4	87.3 ± 8.8

Benchmark results: pixel-based environments

Dataset Type	Dataset	GCIQL	QRL	CRL	HHILP	HIQL	GAS (ours)
Locomotion	visual-antmaze-medium-navigate	19.1 ± 1.6	0.0 ± 0.0	93.7 ± 1.2	94.1 ± 1.2	95.5 ± 0.8	96.4 ± 0.5
	visual-antmaze-large-navigate	4.6 ± 1.9	0.0 ± 0.0	79.5 ± 7.5	85.6 ± 2.5	80.0 ± 2.1	87.0 ± 1.2
	visual-antmaze-giant-navigate	1.5 ± 0.8	0.2 ± 0.8	43.4 ± 5.9	42.4 ± 1.9	34.1 ± 1.0	59.0 ± 2.1
Stitching	visual-antmaze-medium-stitch	4.2 ± 1.6	0.0 ± 0.0	68.0 ± 8.3	92.4 ± 1.2	90.4 ± 4.1	90.0 ± 3.0
	visual-antmaze-large-stitch	0.2 ± 0.3	0.1 ± 0.5	14.7 ± 7.1	33.8 ± 1.2	38.5 ± 5.7	75.2 ± 4.4
	visual-antmaze-giant-stitch	0.0 ± 0.0	0.2 ± 0.6	0.0 ± 0.0	3.6 ± 1.3	0.9 ± 1.1	55.8 ± 3.5
Exploratory	visual-antmaze-medium-explore	0.0 ± 0.0	0.1 ± 0.3	0.0 ± 0.0	0.0 ± 0.0	0.9 ± 1.4	65.9 ± 6.8
	visual-antmaze-large-explore	0.0 ± 0.0	0.0 ± 0.0	0.0 ± 0.0	0.0 ± 0.0	0.0 ± 0.0	15.1 ± 6.8
Manipulation	visual-scene-play	10.6 ± 2.7	13.5 ± 2.8	8.4 ± 0.9	35.6 ± 4.9	47.9 ± 3.9	54.4 ± 6.2

Ablation: Temporal Efficiency Filtering

Dataset	# States in Dataset	TE-Filtered States (%)		# Nodes in Graph		Normalized Return		
		All States	Ours	All States	Ours	All States	Ours	$\Delta \uparrow$
antmaze-giant-navigate	1M	100	6	2092	978	63.4 ± 3.7	77.6 ± 2.9	+14.2
antmaze-giant-stitch	1M	100	8	3490	1966	75.3 ± 5.7	88.3 ± 3.6	+13.0
antmaze-large-explore	5M	100	2	6213	2499	75.4 ± 4.3	94.2 ± 3.0	+18.8
scene-play	1M	100	6	2809	725	63.5 ± 5.5	73.6 ± 8.0	+10.1

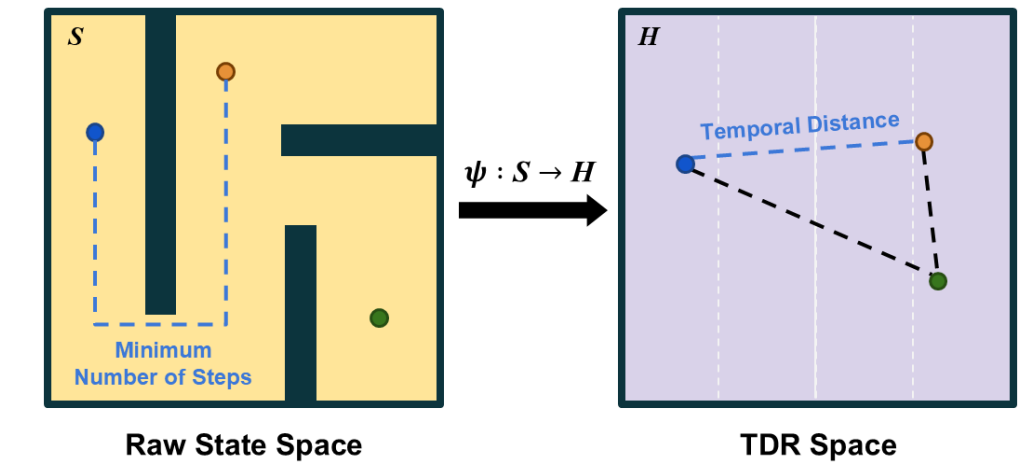
- This table compares the performance of GAS with TE filtering to a variant that constructs the graph from all states **without filtering**.

Performance Highlights

- Q. Does GAS excel at **long-horizon reasoning**?
- A. Yes, GAS shows strong performance on *antmaze-giant-navigate* and *scene-play*, which require substantial long-horizon reasoning capabilities in navigation and manipulation domains, respectively.
- Q. Does GAS demonstrate effective **stitching ability**?
- A. Yes, GAS outperforms baselines on *antmaze-{medium, large, giant}-stitch*, where the datasets consist of short goal-reaching trajectories.
- Q. Can GAS effectively learn from **suboptimal datasets**?
- A. Yes, GAS achieves the best performance on *antmaze-{medium, large}-explore*, where the datasets consist of extremely low-quality data.
- Q. Can GAS effectively handle **image-based tasks**?
- A. Yes, GAS demonstrates strong performance not only in *state-based environments* but also in *pixel-based environments*.

KeyIdeas

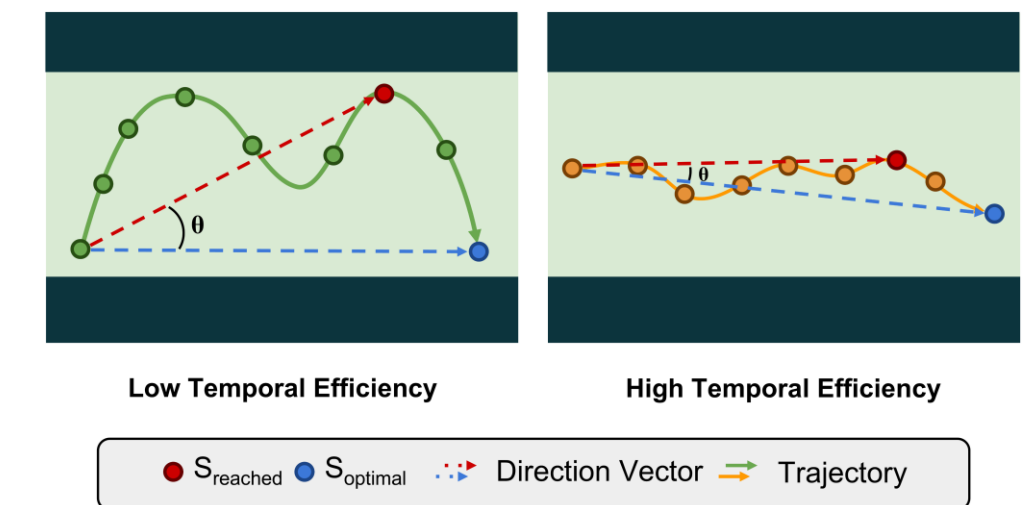
Temporal Distance Representation (TDR)



- TDR_[1] ψ embeds states into a latent space **H**, where the **Euclidean distance** between any two points corresponds to the **minimum number of steps** (i.e., **optimal temporal distance**) required to transition from one state to another in the raw state space **S**.

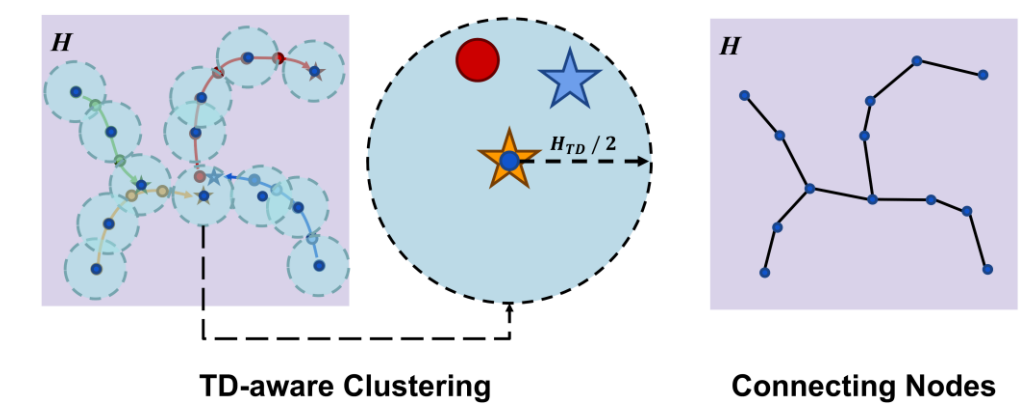
[1] Park et al., "Foundation Policies with Hilbert Representations", ICML 2024.

Temporal Efficiency (TE)



- TE measures the directional alignment between the actual and optimal transitions over a fixed temporal distance.
- (**S_{searched}**: state observed H_{TD} steps after S_{cur})
- (**S_{optimal}**: state at H_{TD} temporal distance from S_{cur})
- Before graph construction, **filtering low-TE states** reduces **construction overhead** and improves **graph quality**.

TD-aware Graph Construction



- GAS clusters states in the TDR space at regular temporal distance intervals H_{TD} , **grouping semantically similar states** from different trajectories.
- Each cluster center becomes a graph node, and edges are added between nodes if their temporal distance is below H_{TD} , enabling **cross-goal stitching** across disconnected trajectories.